

**TLD and Monte Carlo Techniques for  
Reference-Quality Brachytherapy  
Dosimetry  
AAPM Summer School  
23 June 2009**

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# Learning Objectives

- To review the requirements and challenges of quantitative brachytherapy dosimetry
  - Detector selection
  - Roles of experimental and computational dosimetry
- To review the formalism, techniques, and associated uncertainties of
  - current TLD dosimetry practices
  - Current Monte Carlo simulation dose-estimation practices
- To review emerging developments
  - Improved energy-response corrections for TLD-100
  - New detector systems
  - Model-based dose-calculation algorithms

# Potential COI Disclosures

- **Williamson**
  - Research grants supported by Varian and Philips
- **Rivard**
  - Research grants supported by Nucletron, Varian, and IsoRay



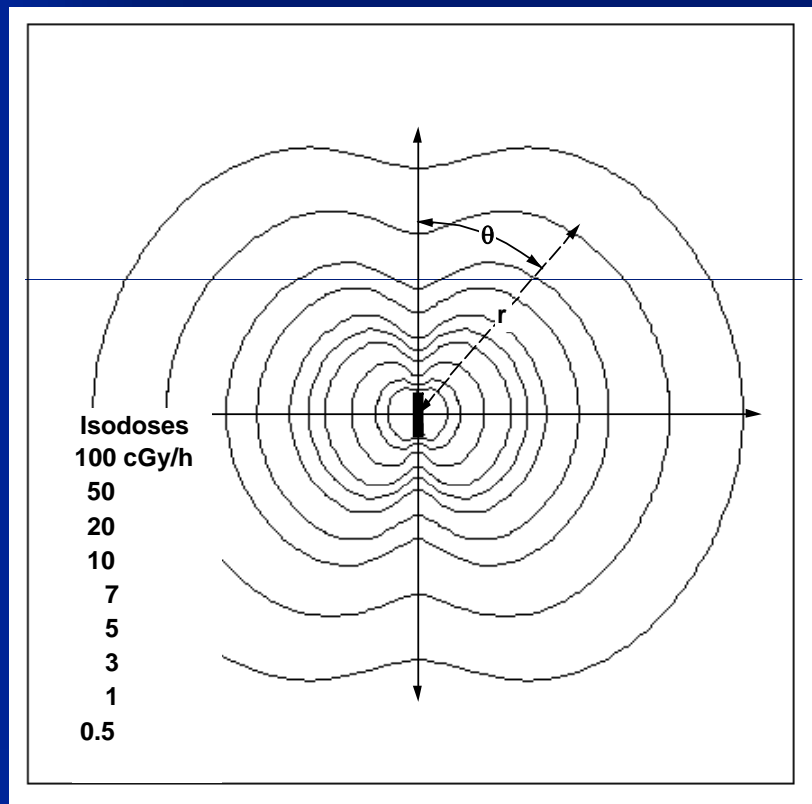
(Radiumhemmet, Stockholm: 1945)

# What is “Quantitative Dosimetry?”

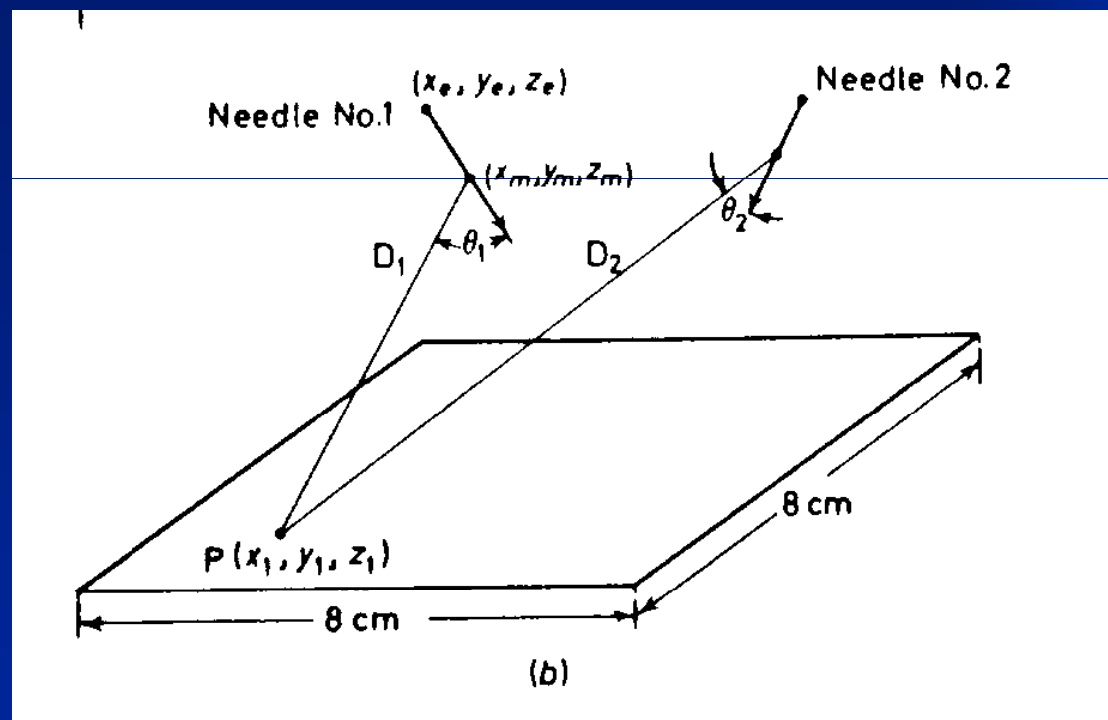
- **Williamson’s definition:** absorbed dose estimation method providing
  - Accurate representation of well-defined physical quality
  - Rigorous uncertainty analysis  $\Rightarrow$   $<10\%$  uncertainty 0.5 to 5 cm in liquid water
  - Traceable to NIST primary standards ( $S_{K,N99}$ )
- **Applications**
  - Single-source dose-rate arrays for TG-43 parameter determination (“Reference quality” dose distributions)
  - Direct treatment planning
  - Validating semi-empirical algorithms

# Single-Source Dose Distributions

## Superposition Model



Single-source dose distribution  
= Dosimetry



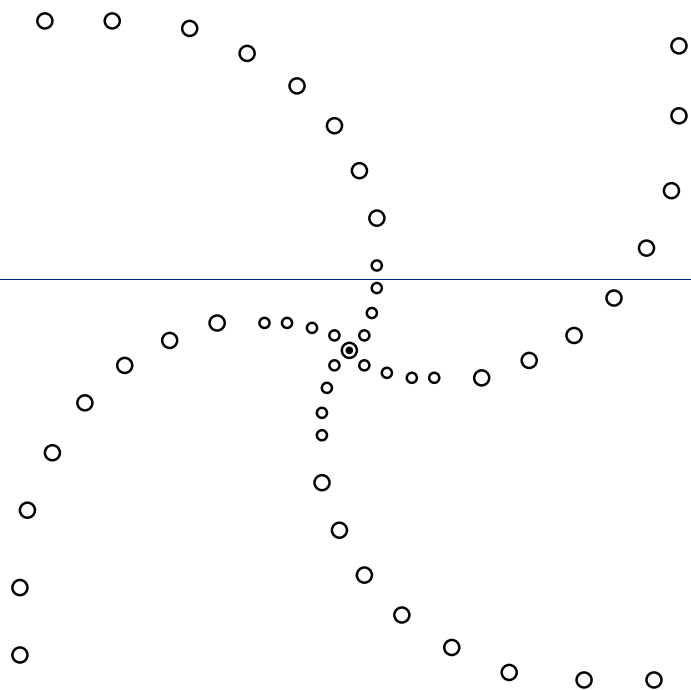
Superposition of multiple source doses  
= Treatment Planning

# Criteria for experimental dosimeters

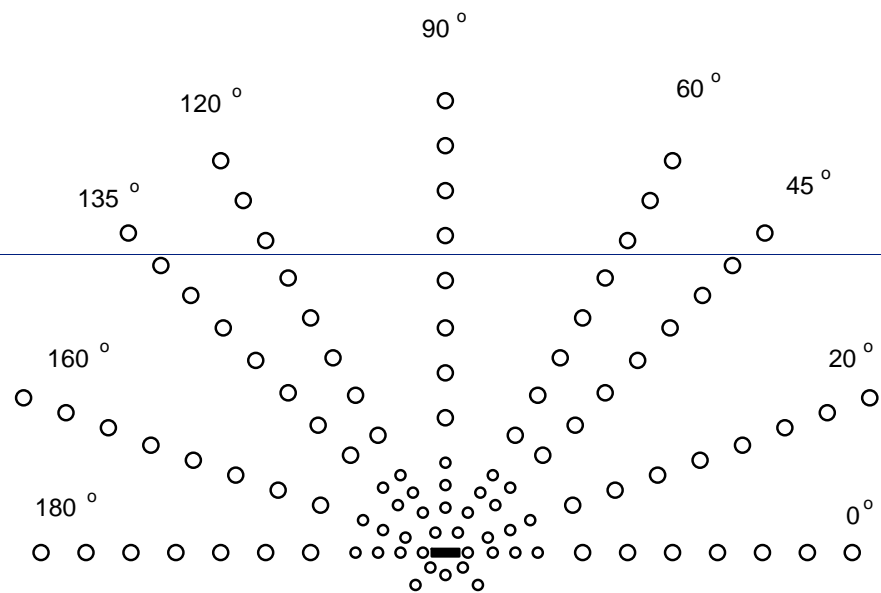
- **Dosimetric environment**
  - Large Dose Gradients
  - Wide Range of Dose Rates
  - Low Photon Energies
- **Signal stability and reproducibility**
  - Spatially and temporally constant Sensitivity (signal/dose)
  - Free of fading, dose-rate effects
- **Small size, high sensitivity, large dynamic range**
  - Small size: avoid averaging dose gradients
  - Large size: Good signal at low doses
- **$\pm 20 \mu\text{m}$  positioning accuracy needed for 2% accuracy**
- **Support measurements at many points**

# Solid Water Phantoms for TLD Dosimetry

Transverse Axis Measurement Phantom



Polar Dose Profile Measurement Phantom



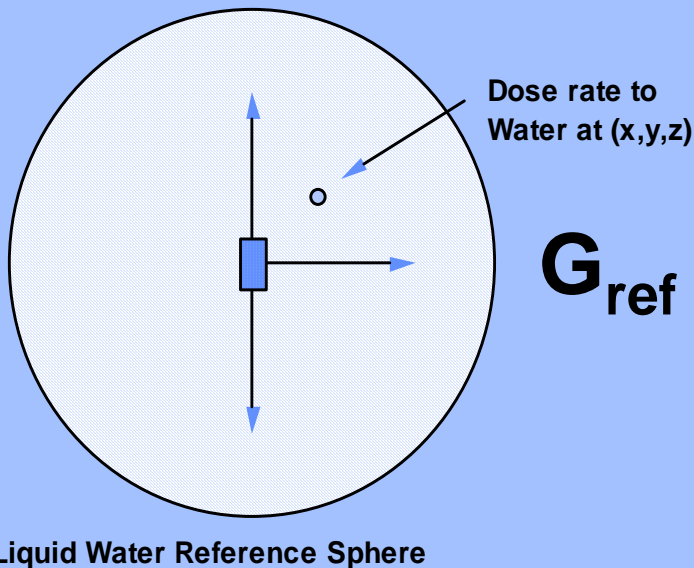
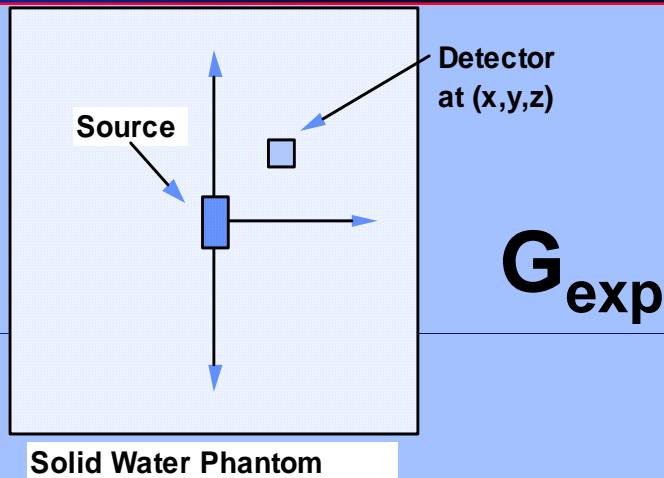
**100-200  $\mu\text{m}$  positional accuracy achievable**

# TLD Detectors

- Use TLD-100 LiF extruded ribbons ('chips')
  - 1 x 1 x 1 mm<sup>3</sup> at distances < 2 cm
  - 3 x 3 x 0.9 mm<sup>3</sup> at distances ≥ 2 cm
- Use RMI 453 Machined Solid Water Phantom
  - Composition (CaCO<sub>3</sub> + organic foam) not stable
  - Either perform chemical assay or use high purity PMMA
- Annealing protocol
  - 1 hour 400° C followed by 24 hours of 80° C pre-irradiation
  - OR
  - 1 hour 400° C pre-irradiation followed by 10 minutes at 100° C Post-irradiation



# Brachytherapy Dosimetry



- **Given:**  $M(r)$  = dosimeter (TLD or Diode) reading in geometry  $G_{exp}$
- **Desired:**  $(\dot{D}_{med}(r)/S_K)$  = absorbed dose rate to water in reference geometry,  $G_{ref}$
- **Many Corrections**
  - Detector sensitivity
  - Phantom vs reference geometry
  - Radiation field Perturbation
  - Detector response artifacts

# Experimental Dose Measurement-I

$$\left[ \frac{\dot{D}_{\text{med}}(r)}{S_K} \right] = \frac{M \cdot k_l(M) \cdot g(\Delta T) \cdot p_{\text{phant}}(r)}{S_K \cdot S_{\text{AD}}(M_0) \cdot S_{\text{AD}}^{\text{rel}}(r)}$$

$$\frac{M(r) \cdot k_l(M \rightarrow M_0) \cdot g(\Delta T) \cdot p_{\text{phant}}(Q_{\text{exp}}, G_{\text{exp}} \rightarrow Q_{\text{ref}}, G_{\text{ref}}; r)}{S_K \cdot S_{\text{AD}}(M_0, Q_0, G_0) \cdot S_{\text{AD}}^{\text{rel}}(Q_0, G_0 \rightarrow Q_{\text{exp}}, G_{\text{exp}}, r)}$$

- $M$  = reading at position  $r$  in geometry  $G_{\text{exp}}$  and spectrum  $Q_{\text{exp}}$
- $S_K$  = Measured Air-Kerma Strength
- $g(T)$  = decay correction over integration interval,  $\Delta T$
- $K_l(M)$  = linearity correction relative to reference level,  $M_0$
- $S_{\text{AD}} = M_0/D_{\text{med}0}$  = absorbed dose sensitivity in calibration beam with geometry  $G_0$  and spectrum,  $Q_0$

# Experimental Dose Measurement-II

$$\left[ \frac{\dot{D}_{\text{med}}(r)}{S_K} \right] = \frac{M \cdot k_l(M) \cdot g(\Delta T) \cdot p_{\text{phant}}(r)}{S_K \cdot S_{\text{AD}}(M_0) \cdot S_{\text{AD}}^{\text{rel}}(r)}$$

- **Relative absorbed dose sensitivity:** corrects for impact of  $G_0/Q_0$  vs.  $G_{\text{exp}}/Q_{\text{exp}}$  differences on dosimeter response

$$S_{\text{AD}}^{\text{rel}}(Q_0, G_0 \rightarrow Q_{\text{exp}}, G_{\text{exp}}, r) = \frac{S_{\text{AD, wat}}(r, M_0, Q_{\text{exp}}, G_{\text{exp}})}{S_{\text{AD, med}_0}(M_0, Q_0, G_0)}$$

- **Phantom correction factor:** impact of  $G_{\text{exp}}/Q_{\text{exp}}$  vs.  $G_{\text{ref}}/Q_{\text{ref}}$  differences on dosimeter response

$$p_{\text{phant, wat}}(Q_{\text{exp}}, G_{\text{exp}} \rightarrow Q_{\text{ref}}, G_{\text{ref}}; r) = \frac{D_{\text{wat}}(r, Q_{\text{ref}}, G_{\text{ref}})}{D_{\text{wat}}(r, Q_{\text{exp}}, G_{\text{exp}})}$$

## TLD readings

$$M(r) = \frac{1}{n} \sum_{i=1}^n \frac{(TL_i - TL_{bkgd})}{S_i}$$

- $TL_i$  is Measured Response of i-th detector at r
- $S_i$  is relative sensitivity of i-th detector derived from reading TLDs exposed to uniform doses
- TG-43 recommends  $n = 5-15$

# Relative Energy Response

$$E(Q_0, G_0 \rightarrow Q_{\text{ref}}, G_{\text{ref}}, r; G_{\text{exp}}) = \frac{S_{\text{AD}}^{\text{rel}}(Q_0, G_0 \rightarrow Q_{\text{exp}}, G_{\text{exp}}, r)}{p_{\text{phant, wat}}(Q_{\text{exp}}, G_{\text{exp}} \rightarrow Q_{\text{ref}}, G_{\text{ref}}; r)}$$

$$= \frac{k_{\text{bq}}^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}}; M_0) \cdot f^{\text{rel}}(Q_0, G_0 \rightarrow Q_{\text{exp}}, G_{\text{exp}}, r)}{p_{\text{phant}}(Q_{\text{exp}}, G_{\text{exp}} \rightarrow Q_{\text{ref}}, G_{\text{ref}}; r)}$$

- Absorbed dose energy dependence

$$f^{\text{rel}}(Q_0, G_0 \rightarrow Q_{\text{exp}}, G_{\text{exp}}, r) \equiv \frac{f(r, Q_0, G_0)}{f(r, Q_{\text{exp}}, G_{\text{exp}})} = \frac{(\bar{D}_{\text{det}}/D_{\text{wat}})(r, Q_{\text{exp}}, G_{\text{exp}})}{(\bar{D}_{\text{det}}/D_{\text{med}_0})(Q_0, G_0)}$$

- Relative intrinsic energy dependence

$$k_{\text{bq}}^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}}; M_0) \equiv \frac{k_{\text{bq}}(M_0, Q_0)}{k_{\text{bq}}(M_0, Q_{\text{exp}})} = \frac{(M_0/\bar{D}_{\text{det}})(r, Q_{\text{exp}}, G_{\text{exp}})}{(M_0/\bar{D}_{\text{det}})(Q_0, G_0)}$$

# Estimation of Energy-Response Corrections

- Theoretical Approximation

$$E_{\text{Thy}}(r; G_{\text{exp}}) \approx \frac{f^{\text{rel}}(Q_0, G_0 \rightarrow Q_{\text{exp}}, G_{\text{exp}}, r)}{p_{\text{phant}}(Q_{\text{exp}}, G_{\text{exp}} \rightarrow Q_{\text{ref}}, G_{\text{ref}}; r)}$$

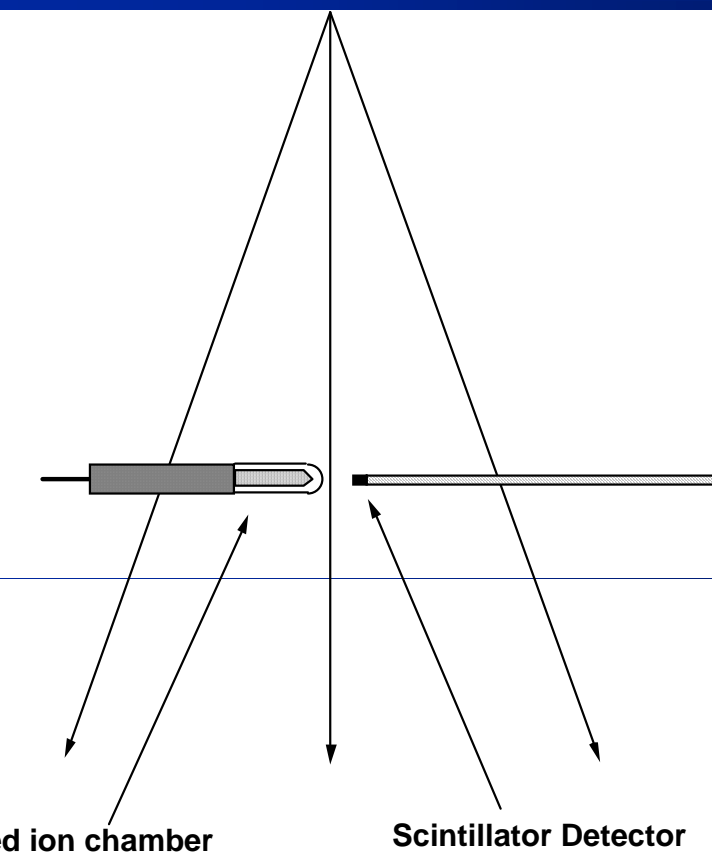
**assuming**  $k_{\text{bq}}^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}}; M_0) \approx 1$

- Direct measurement: x-ray beam with spectrum  $Q_{\text{FS}} \approx Q_{\text{exp}}$

$$E_{\text{meas}}(r; G_{\text{exp}}) = \frac{S_{\text{K,air}}(M_0, Q_{\text{exp}}, G_{\text{FS}})}{S_{\text{AD,med}_0}(M_0, Q_0, G_0)} \times \frac{(K_{\text{air}}/D_{\text{wat}})(Q_{\text{FS}}, G_{\text{FS}})}{p_{\text{disp}}(r, G_{\text{exp}}) \cdot p_{\text{VolAvg}}(r, G_{\text{exp}}) \cdot p_{\text{phant,wat}}(G_{\text{exp}} \rightarrow G_{\text{ref}}; Q_{\text{exp}}, r)}$$

# Compare detector to “matched” X-ray Beam calibration in Free-Air

$Q_{FS} = 40-120 \text{ kVp}$



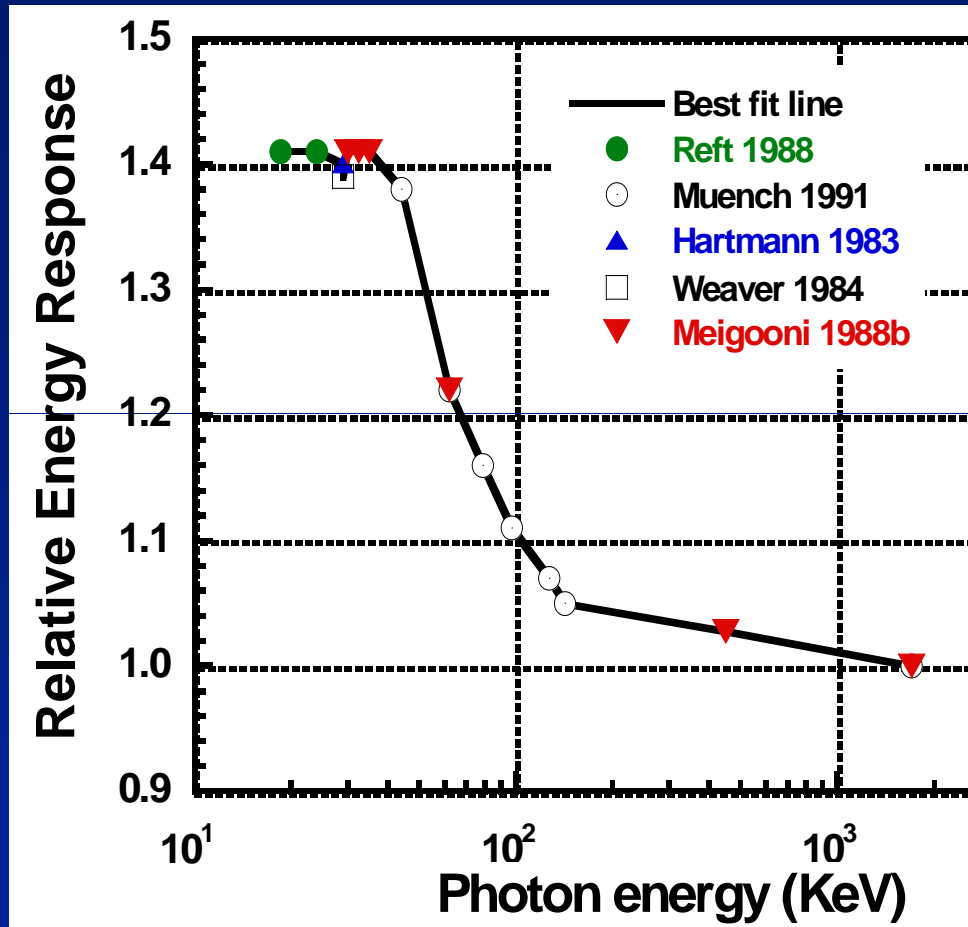
$$S_{K,air}(Q_{FS}) = M(Q_{FS}, G_{FS}) / K_{air}^{FS}$$

$$E(r) = \left( \frac{S_{K,air}(Q_{FS})}{S_{AD}(Q_0)} \right) \cdot \frac{\left( \overline{\mu_{en}/\rho} \right)_{wat}^{air}(Q_{FS})}{p_{VolAvg} \cdot p_{disp}(r) \cdot p_{disp}}$$

$$p_{disp}(G_{FS} \rightarrow G_{exp}) = \frac{D_{wat} \text{ in medium}}{K_{wat}^{FS} \text{ in cavity}} \approx 0.97$$

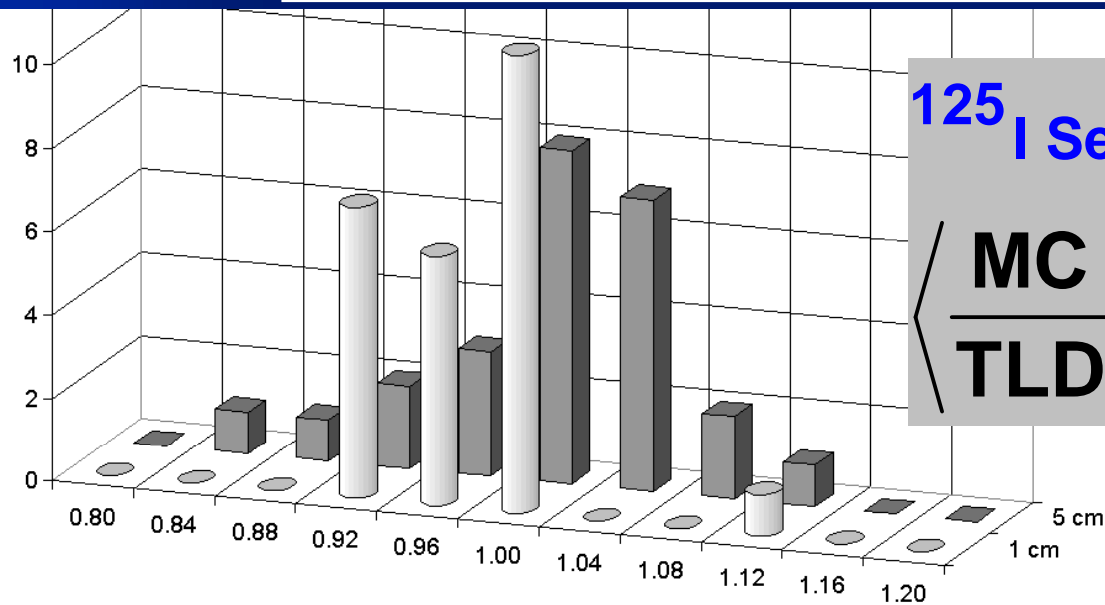
$$p_{VolAvg}(Q_{exp}, G_{exp}) = \frac{D_{wat}(r)}{\overline{D_{wat}}(r)} = \frac{D_{wat}(r) \text{ at point } r}{V^{-1} \int_{V(r)} D_{wat}(r') dV'} \left\} \in (0.80 - 1.00)$$

# Measured TLD-100 relative Energy Response



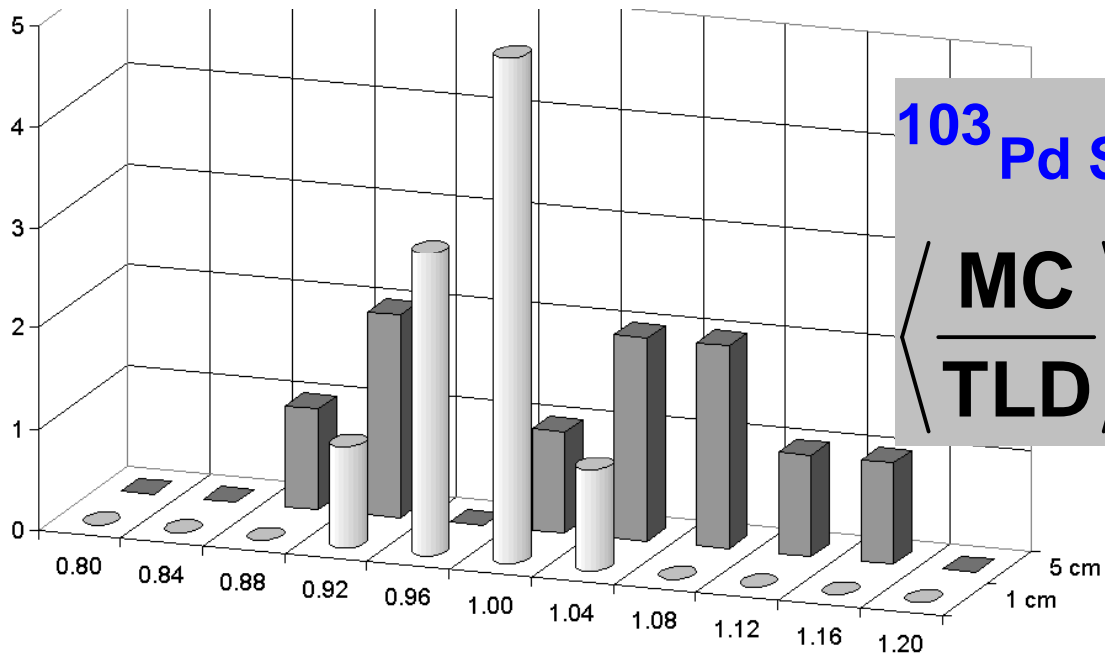


# Monte Carlo vs. TLD Dose Rates



<sup>125</sup>I Seeds: 14 Models and 25 comparisons

$$\left\langle \frac{\text{MC}}{\text{TLD}} \right\rangle = \begin{cases} 0.979 \pm 0.045 & (1 \text{ cm}) \\ 1.002 \pm 0.066 & (5 \text{ cm}) \end{cases}$$

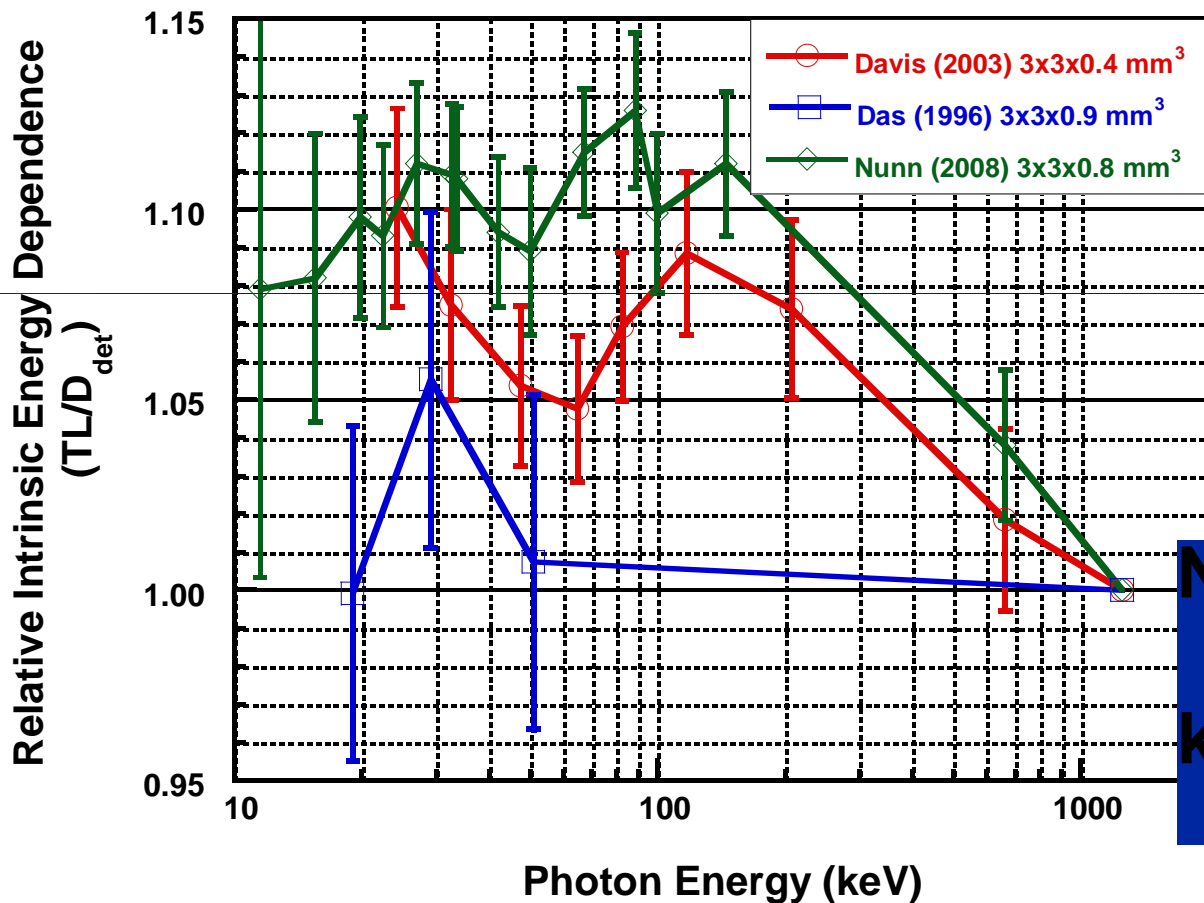


<sup>103</sup>Pd Seeds: 5 Models and 10 comparisons

$$\left\langle \frac{\text{MC}}{\text{TLD}} \right\rangle = \begin{cases} 0.982 \pm 0.028 & (1 \text{ cm}) \\ 1.045 \pm 0.106 & (5 \text{ cm}) \end{cases}$$

# Modern Measurements: $k_{bg} \neq 1$

Nunn 2008, Davis 2003, and Das 1995



$$k_{bq}^{rel}(Q_0 \rightarrow Q) = \frac{S_{K,air}^{rel}(Q_0, G_{fs} \rightarrow Q, G_{fs})}{f_K^{rel}(Q_0, G_{fs} \rightarrow Q, G_{fs})}$$

Nunn-Davis Results

$$k_{bq}^{rel} = \begin{cases} 1.09-1.10 \pm 2\% & 23 \text{ keV} \\ 1.08-1.11 \pm 2\% & 32 \text{ keV} \end{cases}$$

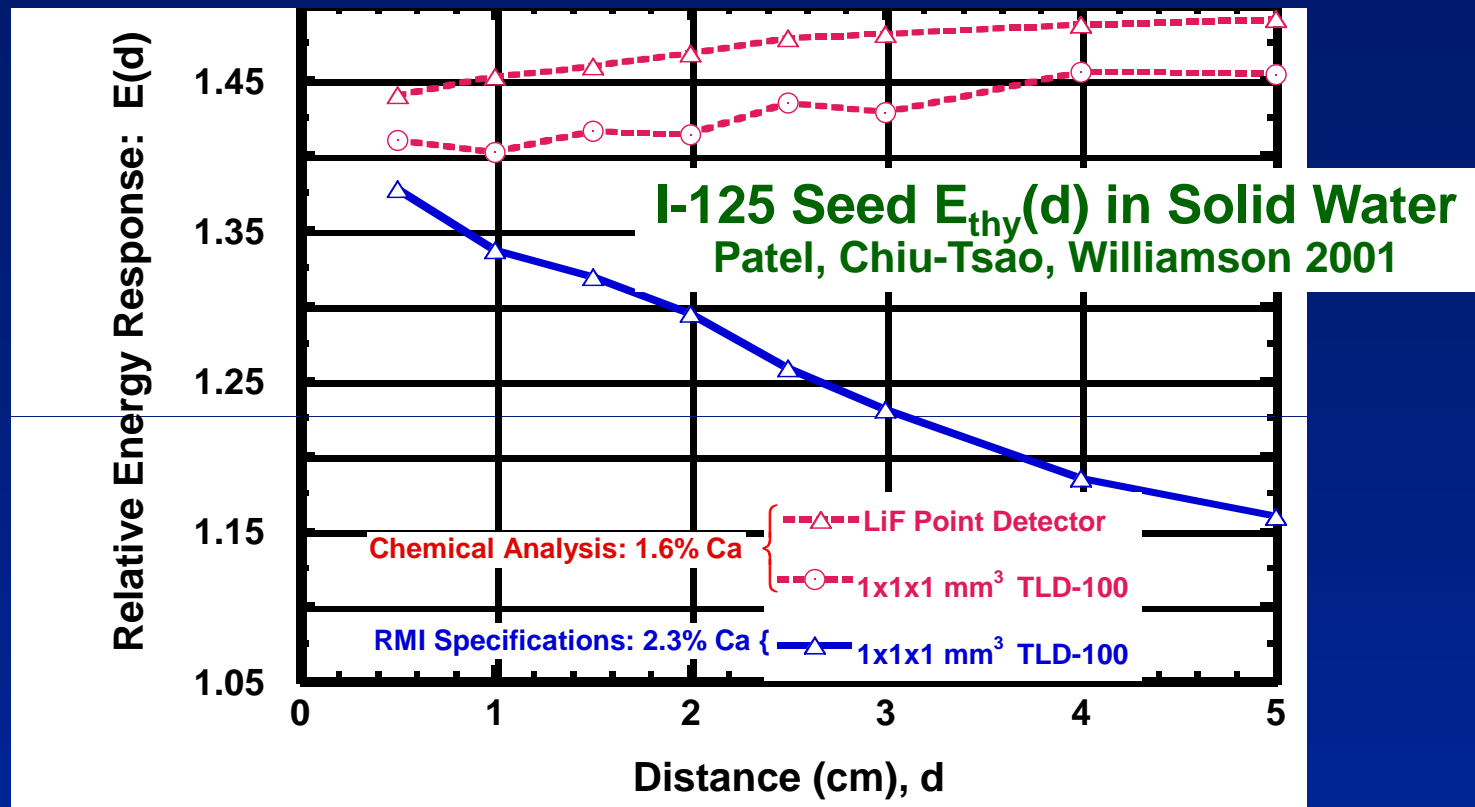
Energy linearity of TLD is controversial

# Impact of $k^{rel}$ Revisions on MC-TLD Agreement

- Rivard comparisons of TLD and MC at 1 cm and 5 cm for  $^{125}\text{I}$  and  $^{103}\text{Pd}$  sources
- Revised  $k_{rel} > 1.05$  will significantly worsen agreement

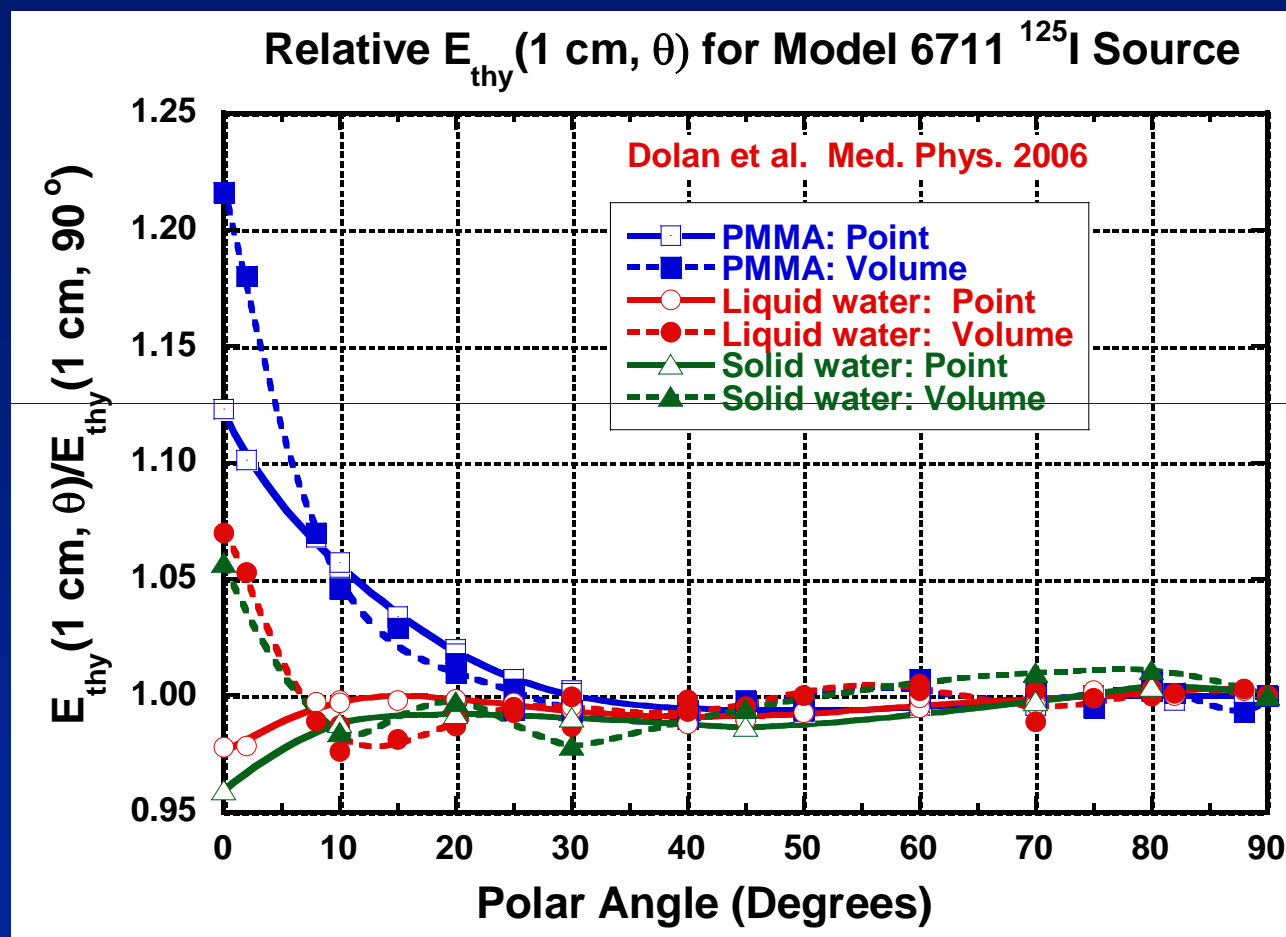
Source	Distance	Monte Carlo/TLD dose rate			
		$K_{bq}^{rel} = 1.00$	$K_{bq}^{rel} = 1.05$	$K_{bq}^{rel} = 1.075$	$K_{bq}^{rel} = 1.10$
$^{125}\text{I}$	1 cm	$0.979 \pm 0.045$	1.028	1.052	1.077
	5 cm	$1.002 \pm 0.066$	1.052	1.077	1.102
$^{103}\text{Pd}$	1 cm	$0.982 \pm 0.028$	1.031	1.056	1.080
	5 cm	$1.045 \pm 0.106$	1.097	1.123	1.150

# Absorbed Dose Energy Response Correction



- $E_{thy}$  is not a constant
  - 4% variation with distance even in water
  - Displacement correction  $\approx$  4% for 1 mm mini-cubes
- Solid-to-Liquid Water correction: 4%-15% at 1-5 cm
  - 10-30% variations in SW [Ca] reported  $\Rightarrow$  5%-20% dosimetric errors

# Absorbed Dose Energy Response Correction



- Up to 22% variation in  $E(r, \theta)$  with polar angle

### TLD uncertainties: $\dot{D}_{\text{wat}}(r)/S_K$ for Model 6711 $^{125}\text{I}$ in PMMA

Component	1 cm distance		5 cm distance	
	$\% \sigma_{x_i}$	Type	$\% \sigma_{x_i}$	Type
TLD reading statistics	1.3%	A	2.2%	A
TLD calibration (including Linac calibration)	1.8%	A+B	1.8%	A+B
$f^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}}, r)$ and $p_{\text{phant}}(G_{\text{exp}} \rightarrow G_{\text{ref}}, r)$	0.7%	B	1%	B
Seed/TLD positioning ( $\Delta d = 100 \mu\text{m}$ )	1.2%	B	0.2%	B
$k_{\text{bq}}^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}})$	5%	B	5%	B
NIST $S_K$ + one local transfer	1%	B	1%	B
Combined std. uncertainty ( $k = 1$ )	5.7%		5.9%	

### Monte Carlo uncertainties: Model 6711 seed in liquid water

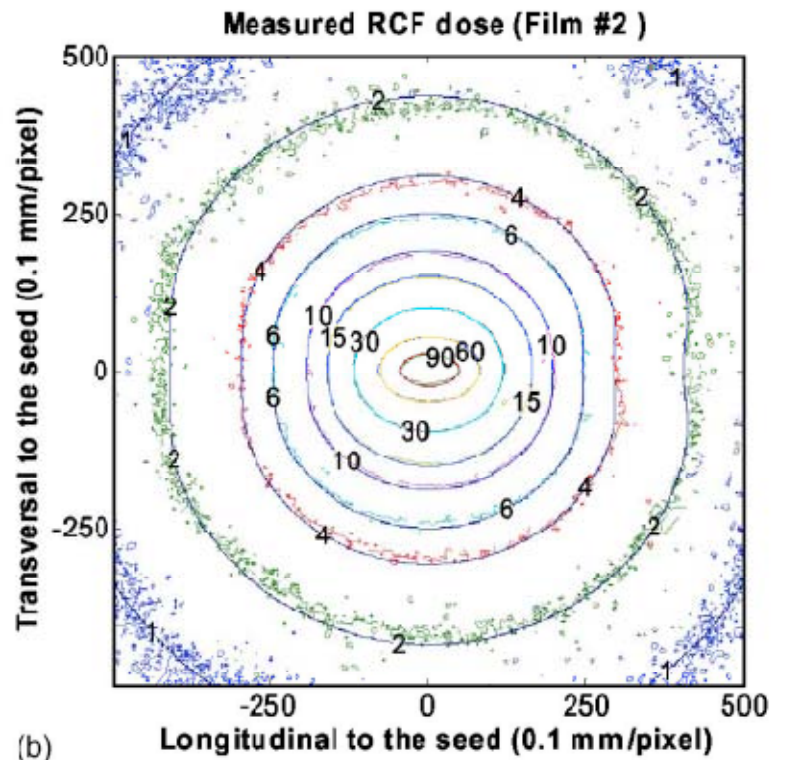
Distance	1 cm	5 cm	10 cm
Statistics	0.2%	0.3%	0.7%
Photon cross-sections	0.7%	2.4%	4.1%
Seed geometry	1.1%	0.9%	0.8%
Source energy spectrum	0.2%	0.3%	0.5%
Combined std. uncertainty ( $k=1$ )	1.3%	2.6%	4.3%

Adapted from Dolan et al. Med Phys 2006

## Other dosimetry systems

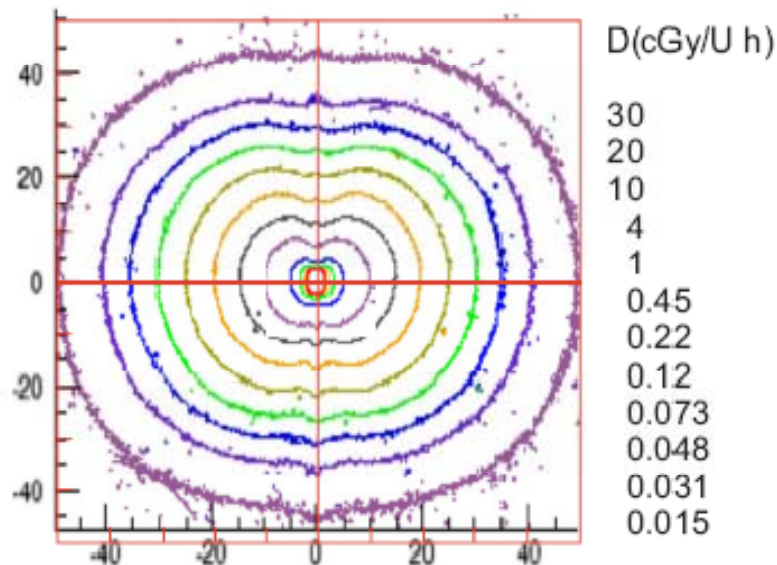
- **Single element detectors**
  - High sensitivity, small size, good SNR, and waterproof
  - Plastic scintillator
    - » Used as transfer/relative dosimeters for beta sources
    - » Large (30%) energy nonlinearity
  - Diode: underutilized in presenter's opinion
    - » Energy linearity well established
    - » Large  $E(d)$  variation for medium energy sources
    - » Established as relative dosimeter for low-energy
- **2D/3D dosimetry media**
  - Radiochromic film and polymer gels
  - Improved positional accuracy and spatial resolution

# Radiochromic Film



- Le and Williamson 2006
  - MD-55-2 RCF with LDR  $^{137}\text{Cs}$  source
  - 6 day exposure
  - Uncertainty ( $k = 1$ )  $< 3.4\%$  for  $D > 5$  Gy, 0.1 mm spatial resolution, double-exposure technique
  - Agreement with MC  $\approx 3\%$

- Chiu-Tsao 2008
  - EBT RCF with Model 3500  $^{125}\text{I}$  seed
  - 0.6 to 279 h exposures
  - Relative dose mapping ( $k=1$ ) uncertainty  $\approx 4\%$  at 0.2 mm spatial resolution
  - Good agreement with TG-43





## Summary: TLD phantom dosimetry

- 1-3 mm size  $\Rightarrow$  precision: 2-5% above 1 cGy
- Energy response corrections
  - Distance independent, excluding phantom corrections
  - Value of  $k_{bq}$  is controversial (<10%)
  - Highly approximate  $f_{rel}$  values are routinely used
- Widely-used SW phantom has uncertain composition
  - High-purity industrial plastics recommended
- Extensive benchmarking of TLD vs Monte Carlo
  - 2-10% agreement for Pd-103 and I-125 sources
  - 6%-10% absolute dose measurement uncertainty

# Basic Discrete Event Monte Carlo Algorithm

Randomly select  
Location, direction  
& energy of primary  
photon

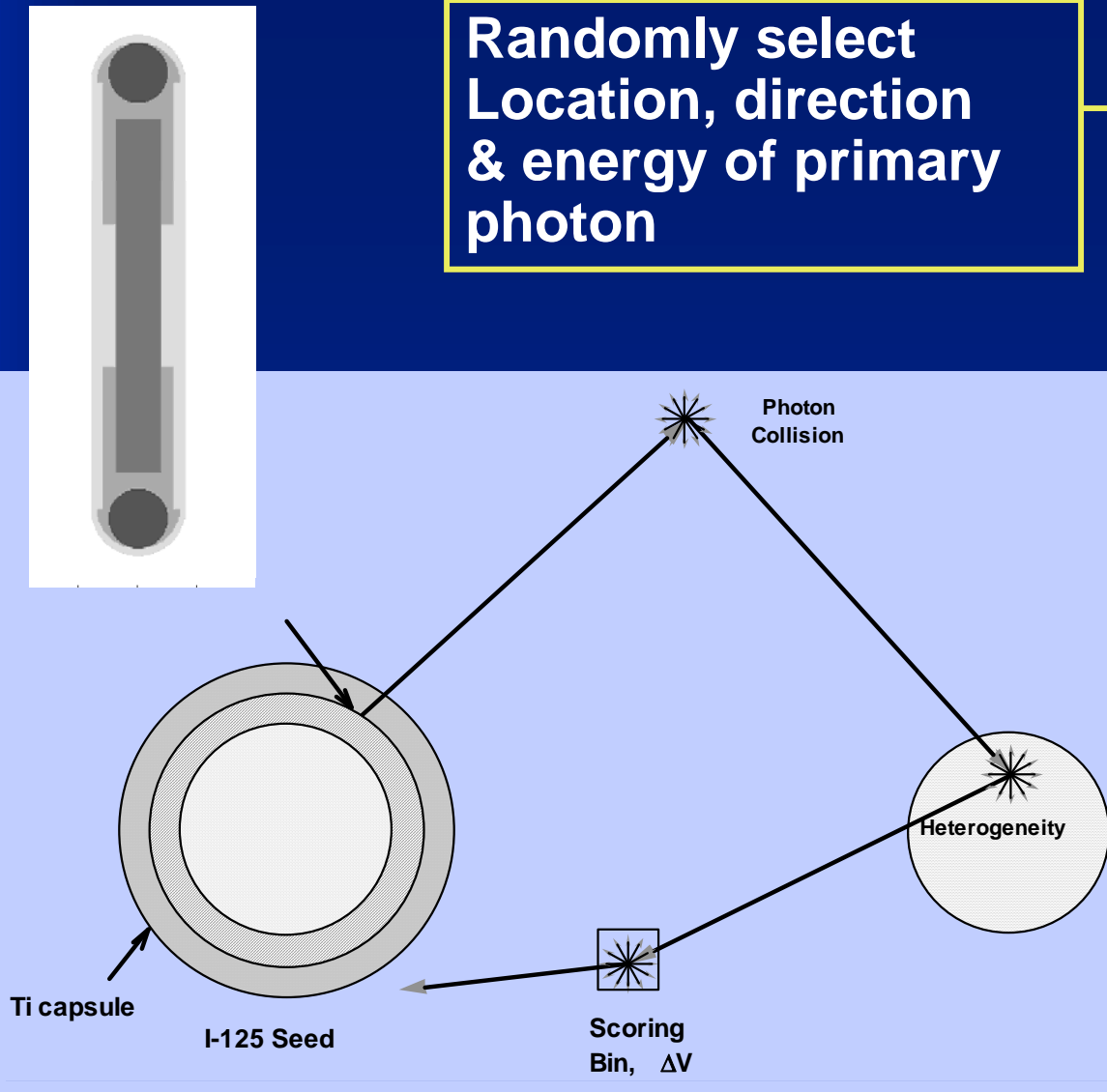
select distance to  
next collision

Select type of  
collision

Select type of  
collision

Select Energy and  
angle of photon  
leaving collision

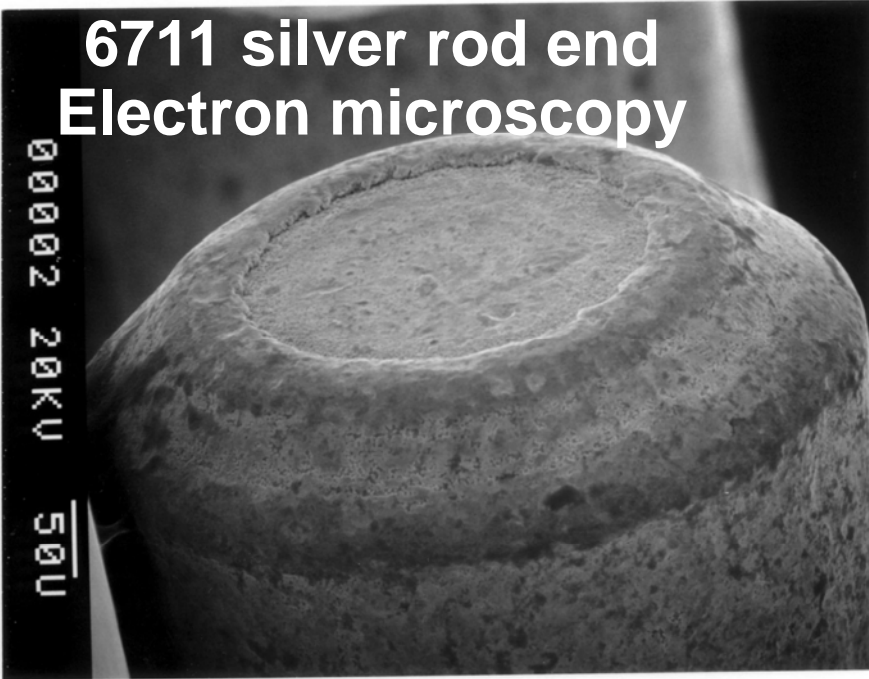
Score collision's  
dose contribution



# Collisional Physics Requirements for Low-Energy Brachytherapy

- Only photon transport needed
  - Secondary CPE obtains (Dose  $\approx$  Kerma)
  - Neutral-particle variance reduction techniques useful
- Comprehensive model of photon collisions
  - NIST EXCOM or EPDL97 Cross sections are essential!!
  - Coherent scattering and electron binding corrections
    - » Use molecular/condensed medium form factors
  - Characteristic x-ray emission from photo effect
- Options: MCNP, EGSnrc, VCU's PTRAN\_CCG, GEANT, Penelope

**6711 silver rod end  
Electron microscopy**

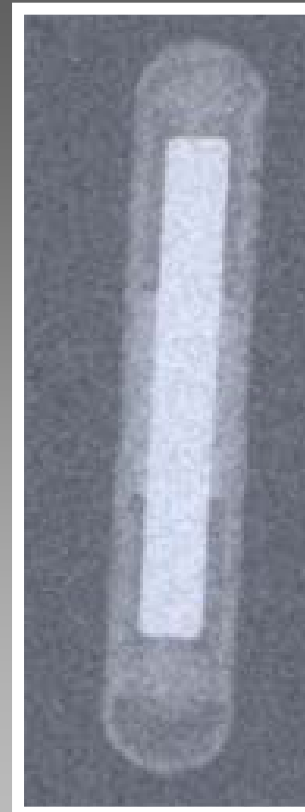


**6711 contact radiographs**

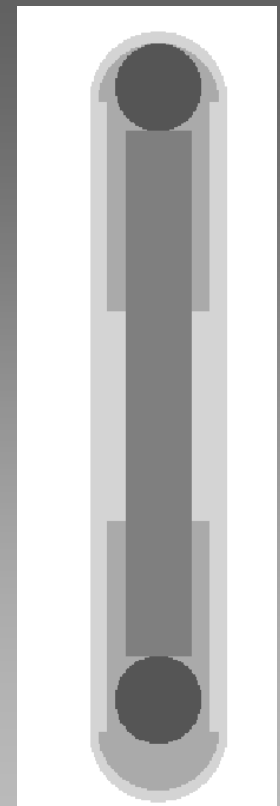


## **Geometric Model Validation**

**DraxImage I-125 Seed**



**Contact  
Radiograph**



**Final Model**

# Calculation of TG-43 Parameters by MCPT

**MCPT calculates per disintegration within source:**

- Dose to medium,  $\Delta D_{\text{med}}(r)$ , near source in phantom geometry: usually 30 cm liquid water sphere
- Air-kerma strength,  $\Delta S_K$ , in free-air geometry usually 5 m air sphere or detailed model of calibration vault

$$\Lambda = \frac{\Delta D_{\text{wat}}(r = 1 \text{ cm}, \theta = \pi / 2)}{\Delta S_K}$$

$$g(r) = \frac{\Delta D_{\text{wat}}(r, \pi / 2) \cdot G(1 \text{ cm}, \pi / 2)}{\Delta D_{\text{wat}}(1 \text{ cm}, \pi / 2) \cdot G(r, \pi / 2)}$$

# Analog and Tracklength Dose Estimation

Need cubic array of voxels:

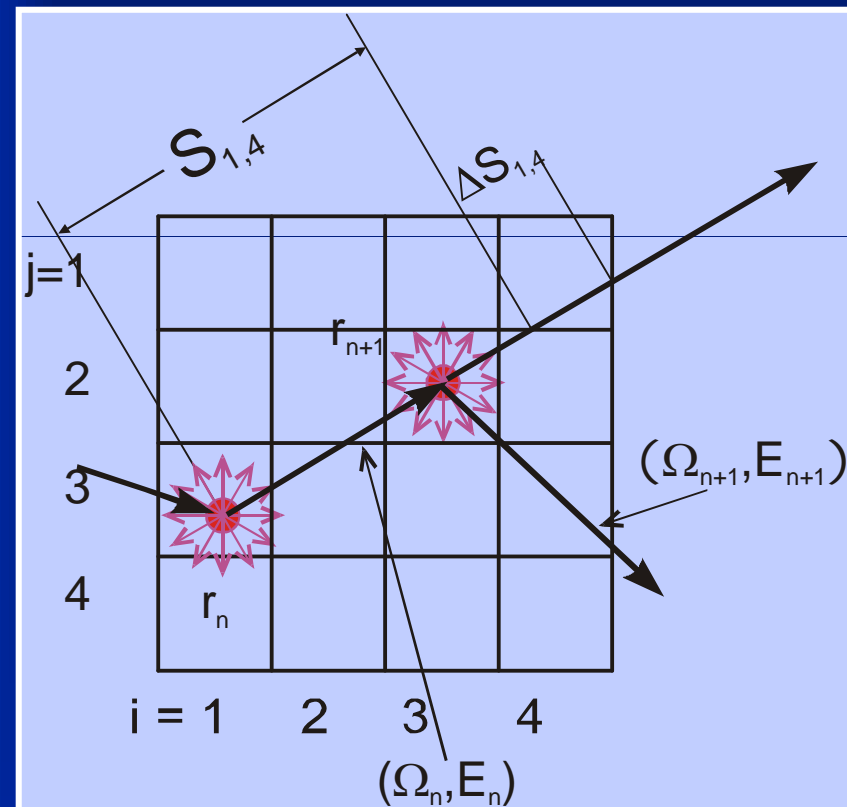
$1 \times 1 \times 1 \text{ mm}^3$  to  $2 \times 2 \times 2 \text{ mm}^3$

Analogue Estimator (EGS method)

$$D_{2,3} \text{ from } n+1 = \frac{\text{Energy in} - \text{Energy out}}{\text{voxel mass}}$$

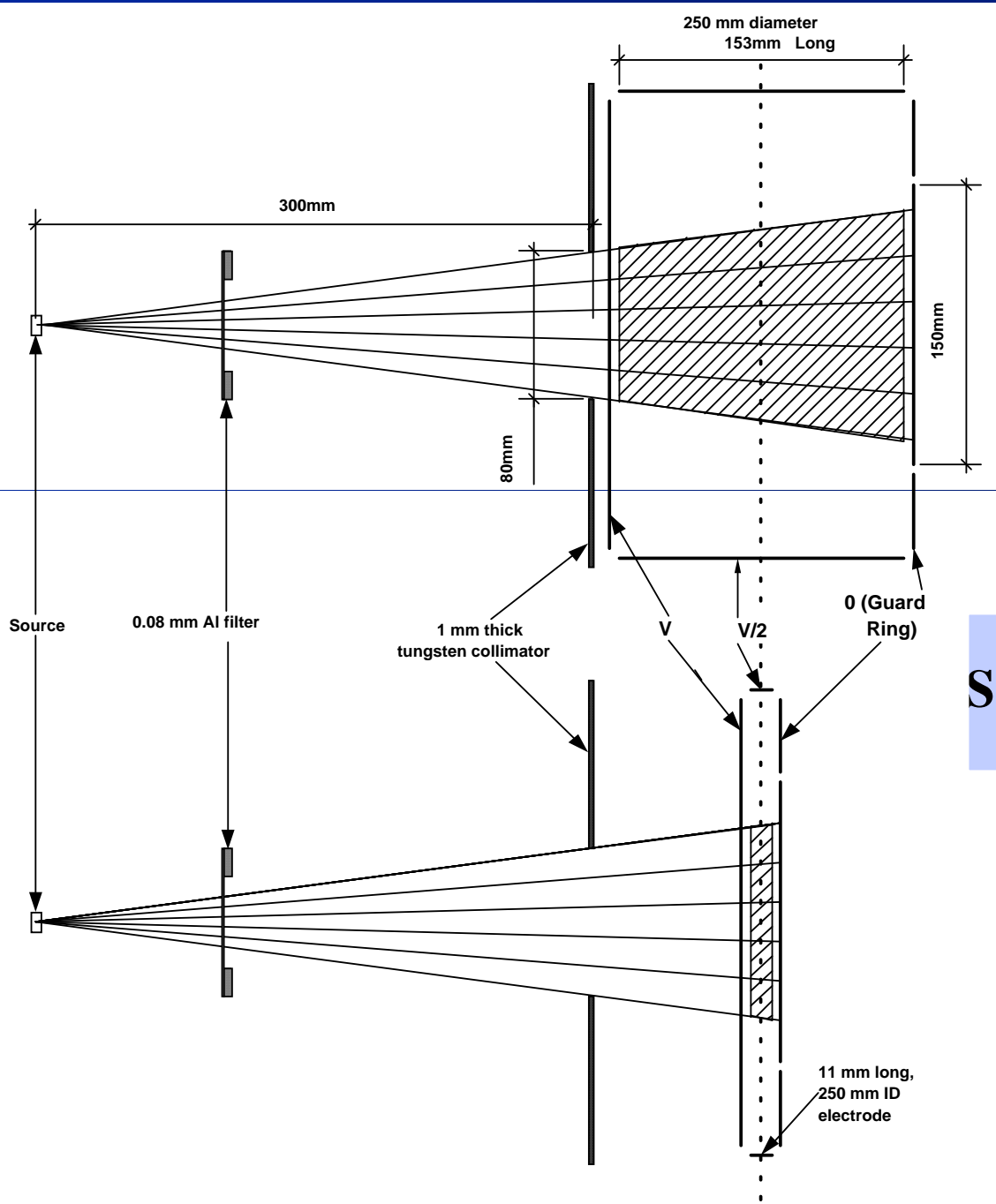
Expected Value Tracklength Estimator

$$D_{1,4} \text{ from } n \propto E_n \cdot \frac{\Delta S_{1,4}}{\text{voxel volume}} \cdot (\mu_{\text{en}}/\rho)$$



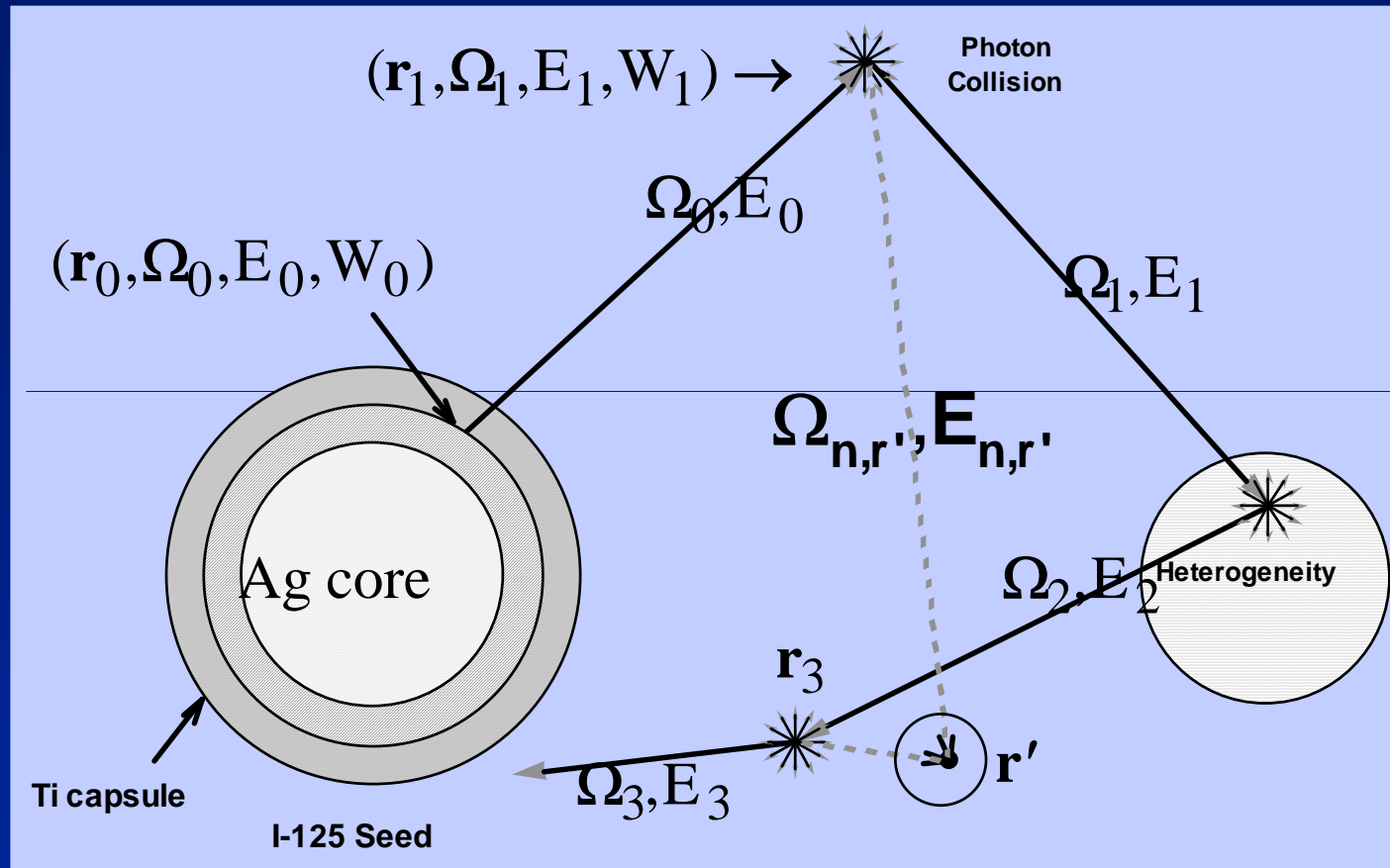
# Wide-angle Free Air Chamber

NIST Primary Standard  
interstitial sources  
photons < 50 keV



$$S_{K,99N} = \frac{(I_{153} - I_{11})d^2}{\rho_{\text{air}}(V_{153} - V_{11})} (W/e) \prod_i k_i$$

# Kerma at a Point: Next Flight Estimator



$$\Delta D(\mathbf{r}') \text{ from } n \propto p(\Omega_{n,r'}) \cdot E_{n,r'} \cdot (\mu_{\text{en}} / \rho) \cdot \frac{e^{-\mu \cdot |\mathbf{r}' - \mathbf{r}_n|}}{|\mathbf{r} - \mathbf{r}_n|^2}$$



## Calculation of $\Delta S_K$ Extrapolated Point-Kerma method

- Place sealed source model at center of large air sphere
- Calculate air-kerma/disintegration,  $\Delta K_{\text{air}}(d)$ , as function transverse axis distance,  $d$
- Extrapolate to free-space geometry by curve fitting

$$\Delta \dot{K}_{\text{air}}(d) \cdot d^2 = \Delta S_K \cdot (1 + \alpha d) \cdot e^{-\mu d}$$

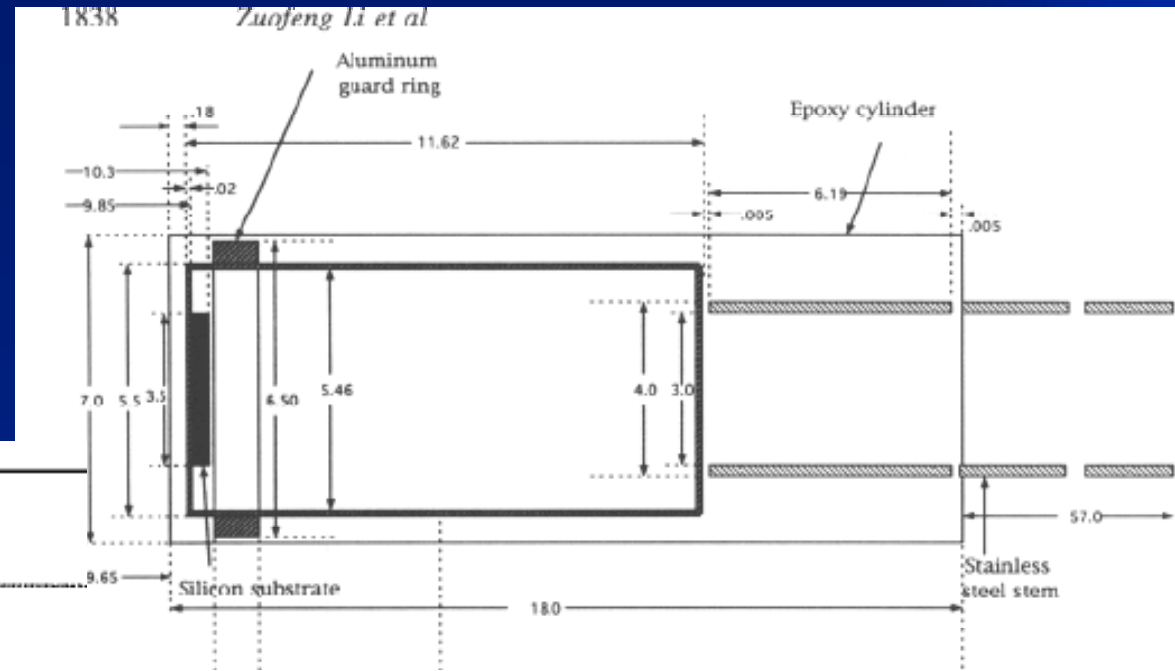
Where  $\Delta S_K$  and  $\alpha$  are unknowns

$(1 + \alpha d)$  - SPR accounts for scatter buildup

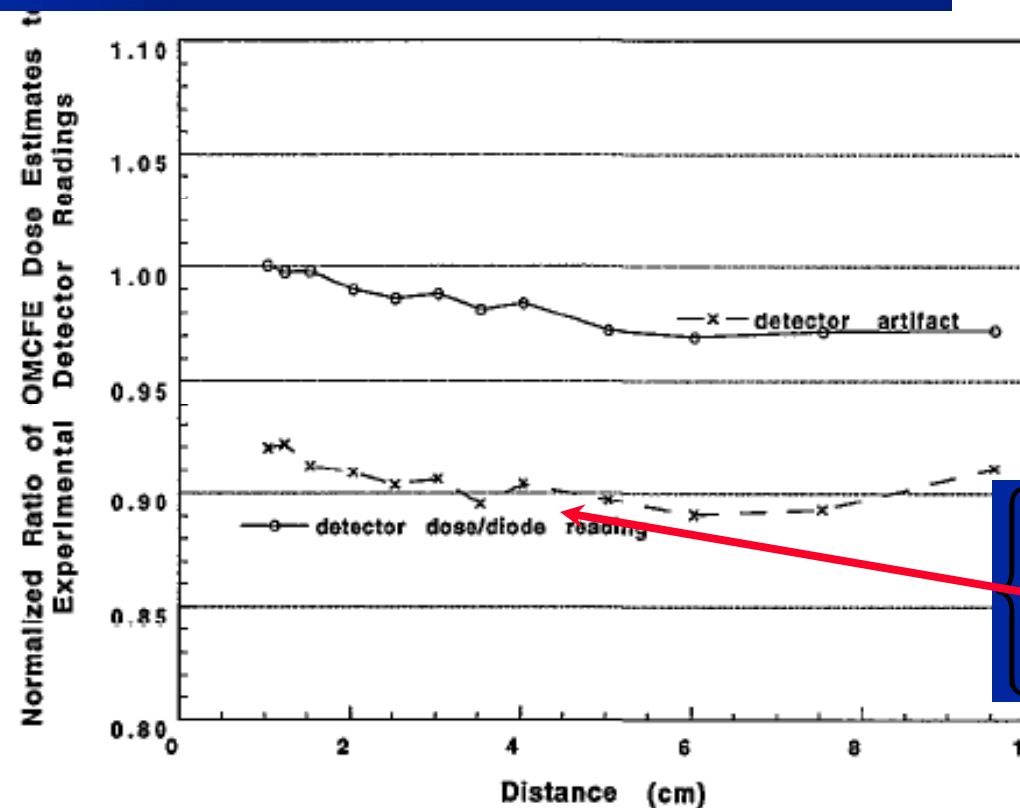
$\mu$  = primary photon attenuation coefficient

# Next-Flight Estimator Application

Use point dose at center of 60  $\mu\text{m}$  x 3 mm Si active volume to approximate  $\bar{D}$



**Scanditronix Electron Field Diode**  
**Monte Carlo Model**  
 Li & Williamson, PMB 1993



$$\frac{1}{k_{bg}(d)} = \left[ \frac{\bar{D}(d)}{M(d)} \right]_{MC} \approx \left[ \frac{D_{NF}(d)}{M(d)} \right]_{MC}$$

# Monte Carlo quantities and estimators for typical seed study

$\Delta D_{\text{wat}}$  (cGy/simulated photon):  $\left\{ \begin{array}{l} \text{Transverse axis} \\ \text{angular dose profiles} \end{array} \right.$

Next-flight estimator for all distances

Track-length estimator for RTP voxel grid

$\Delta E_{\text{ab}}$  Energy imparted to WAFAC volume/simulated photon

Track-length estimator when fluence varies over detector

Next-flight point dose estimator for TLD/diode detectors

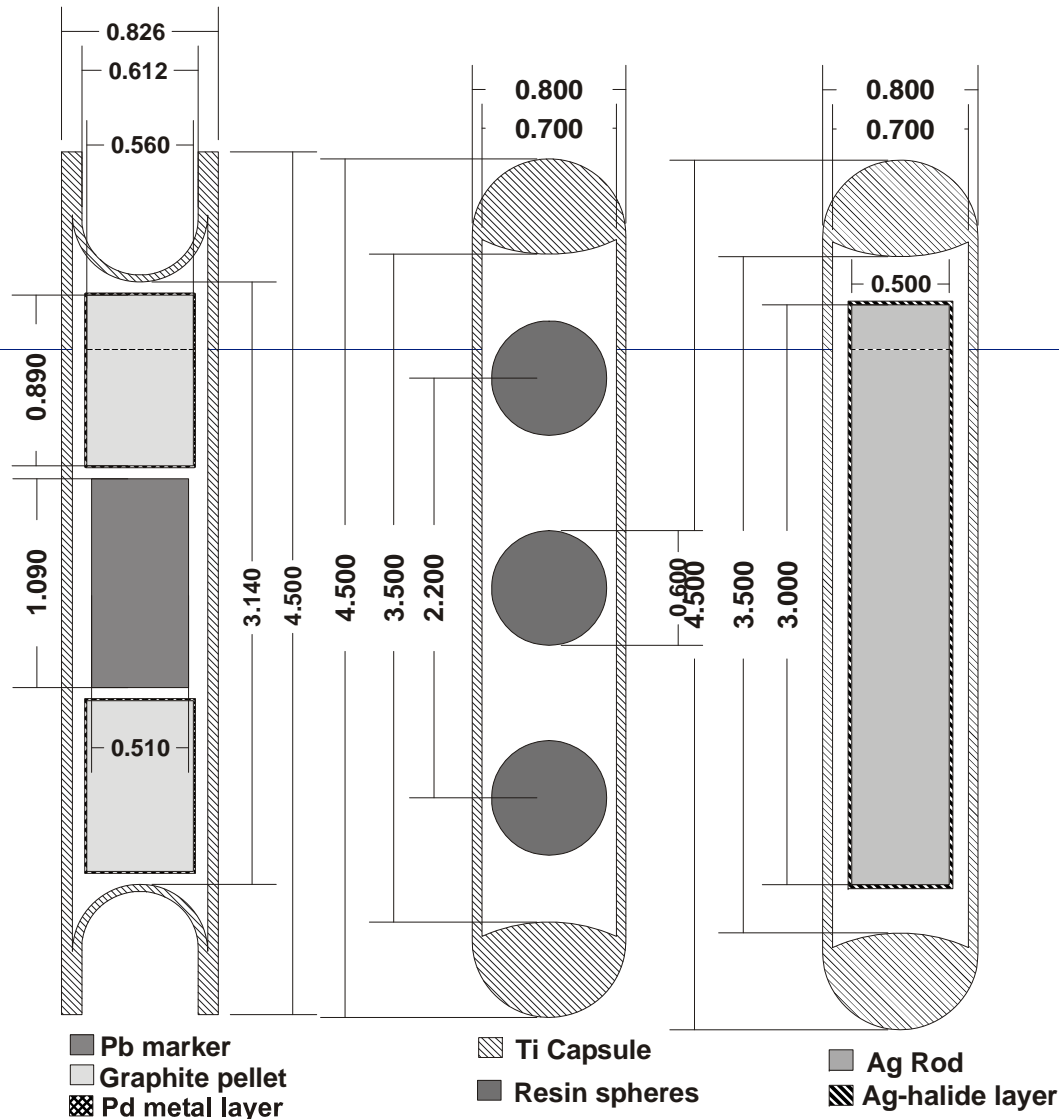
> 2 cm from source

$\Delta K_{\text{air}}$  at geometric points  $\left\{ \begin{array}{l} \text{Transverse-axis} \\ \text{in free air} \quad \text{angular fluence profile (30 cm)} \end{array} \right.$

Track length for WAFAC

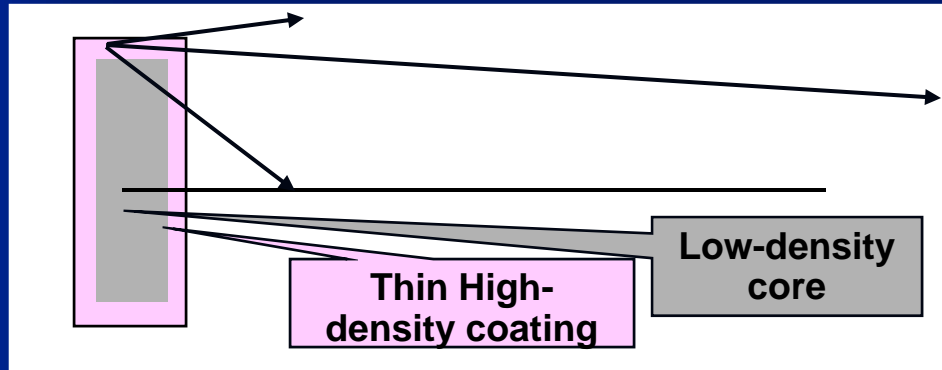
Next-flight for transverse axis distribution

# Models 200 ( $^{103}\text{Pd}$ ), 6702 ( $^{125}\text{I}$ ) and 6711 ( $^{125}\text{I}$ ) Seeds

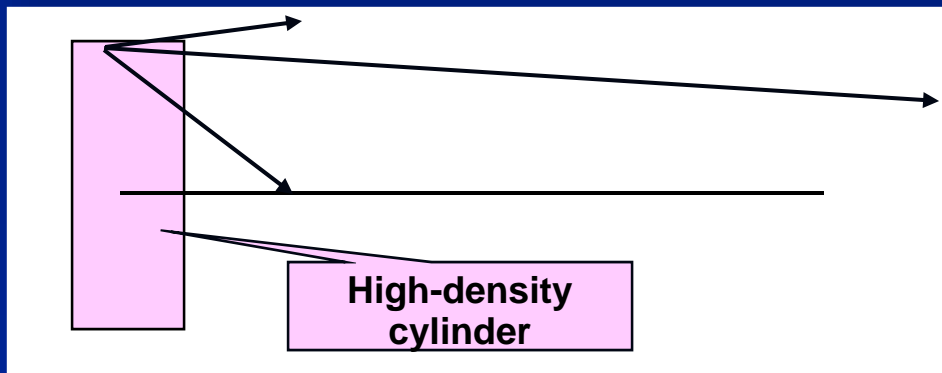


- **Model 200**
  - $^{103}\text{Pd}$  distributed in thin (2-25  $\mu\text{m}$ ) Pd metal coating of right circular graphite cylinder
- **Model 6702**
  - $^{125}\text{I}$  distributed on surface of radio transparent resin spheres
- **Model 6711**
  - $^{125}\text{I}$  distributed in thin ( $\approx 3 \mu\text{m}$ ) silver-halide coating of right circular Ag cylinder

# Sharp corners and opaque coatings

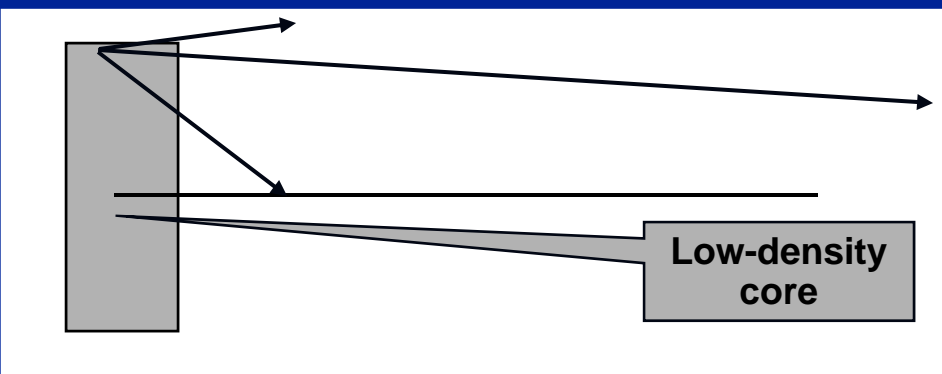


**Near transverse-axis:**  
**Anisotropic at long distances**  
**Isotropic at short distances**  
**Inverse square-law deviations**



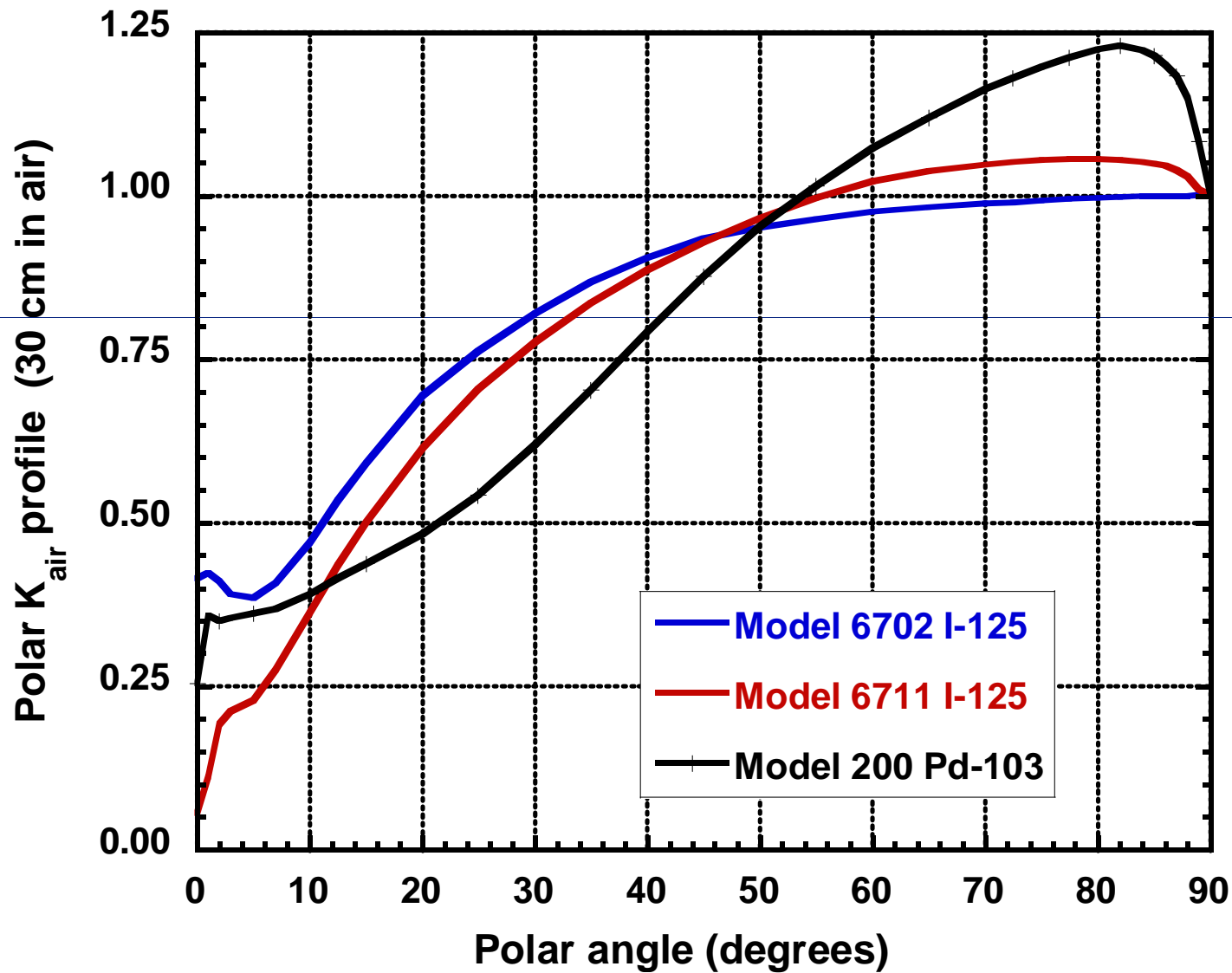
**Anisotropic at long and short distances**  
**Circular ends contribute at**

$$\theta = \tan^{-1} \left[ \frac{L}{2 \times d} \right] = \begin{cases} 8^\circ & d = 1 \text{ cm} \\ 0.3^\circ & d = 30 \text{ cm} \end{cases}$$



**Isotropic at both long and short distances**

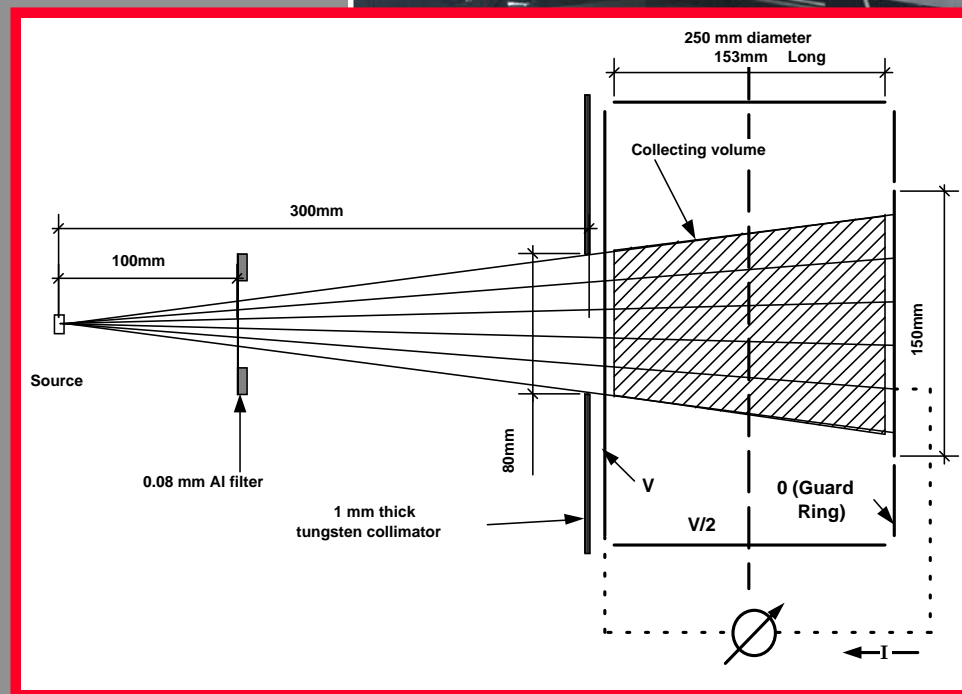
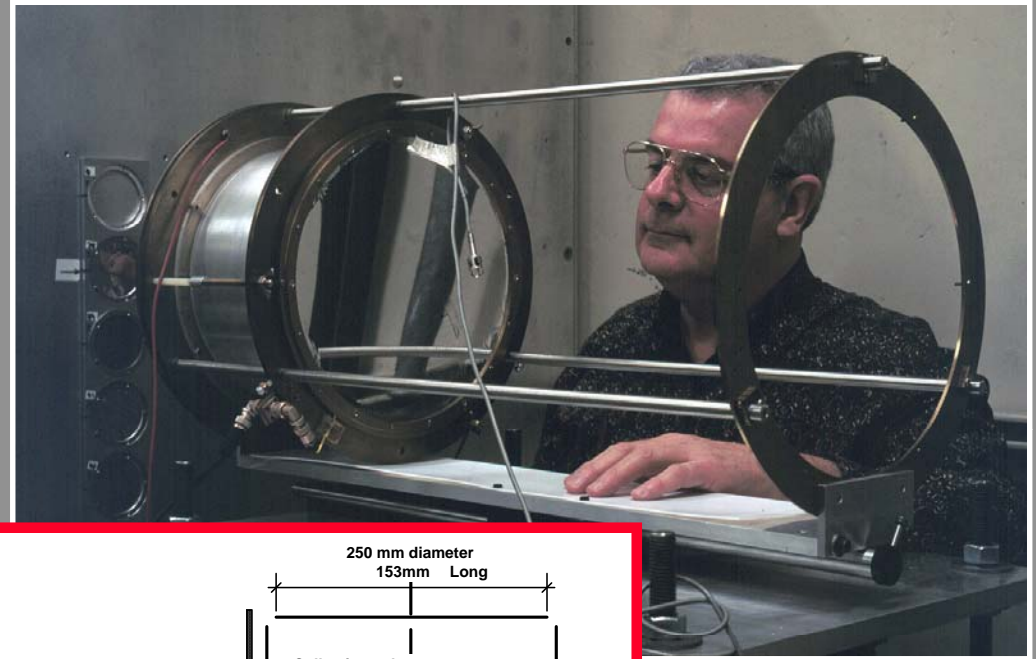
# Polar Anisotropy in Air (30 cm)



# 'WAFAC:' Wide Angle Free-Air Chamber



Rotating Seed Holder



# WAFAC Simulation Method

$$\Delta S_K = \frac{(\Delta E_{ab}^{153} - \Delta E_{ab}^{11}) \cdot d^2}{\rho_{air} \cdot (V_{153} - V_{11})} \cdot k_{inv} \cdot k_{att}$$

where  $\Delta E_{ab}^x$  = Energy absorbed/disintegration in WAFAC volume of length x  
 $d = 38 \text{ cm} = \text{seed-to-WAFAC volume center}$

$$k_{att} = \frac{(\Delta S_K)_{extr}}{k_{inv} \cdot (\Delta K \cdot d^2)_{WFC}} \left\} \text{for a point source} = \begin{cases} 1.025 & \text{Pd-103} \\ 1.013 & \text{I-125} \end{cases}$$

$$k_{inv} = \text{inverse-square correction} = \frac{\int_A \Phi(\ell) \cdot dA}{\Phi(d) \cdot A} = 1.0089$$



# Pd-103 Dose-Rate Constants

Source	Investigator	$\Lambda_{xxD,N99S}$		
		TLD	MC Extrap.	MC WAFAC
Point	Monroe 2002	—	0.683	0.683
Model 200 (light)	Monroe 2002 Nath 2000	--- 0.684	0.797	0.691
Model 200 (heavy)	Monroe 2002 ICWG 1989	----- 0.65	0.744	0.694
NAS MED 3633	Li Wallace 1998	0.693 0.68	0.677	---

## TLD uncertainties: $\dot{D}_{\text{wat}}(r)/S_K$ for Model 6711 $^{125}\text{I}$ in PMMA

Component	1 cm distance		5 cm distance	
	$\% \sigma_{x_i}$	Type	$\% \sigma_{x_i}$	Type
TLD reading statistics	1.3%	A	2.2%	A
TLD calibration (including Linac calibration)	1.8%	A+B	1.8%	A+B
$f^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}}, r)$ and $p_{\text{phant}}(G_{\text{exp}} \rightarrow G_{\text{ref}}, r)$	0.7%	B	1%	B
Seed/TLD positioning ( $\Delta d = 100 \mu\text{m}$ )	1.2%	B	0.2%	B
$k_{\text{bq}}^{\text{rel}}(Q_0 \rightarrow Q_{\text{exp}})$	5%	B	5%	B
NIST $S_K$ + one local transfer	1%	B	1%	B
Combined std. uncertainty ( $k = 1$ )	5.7%		5.9%	

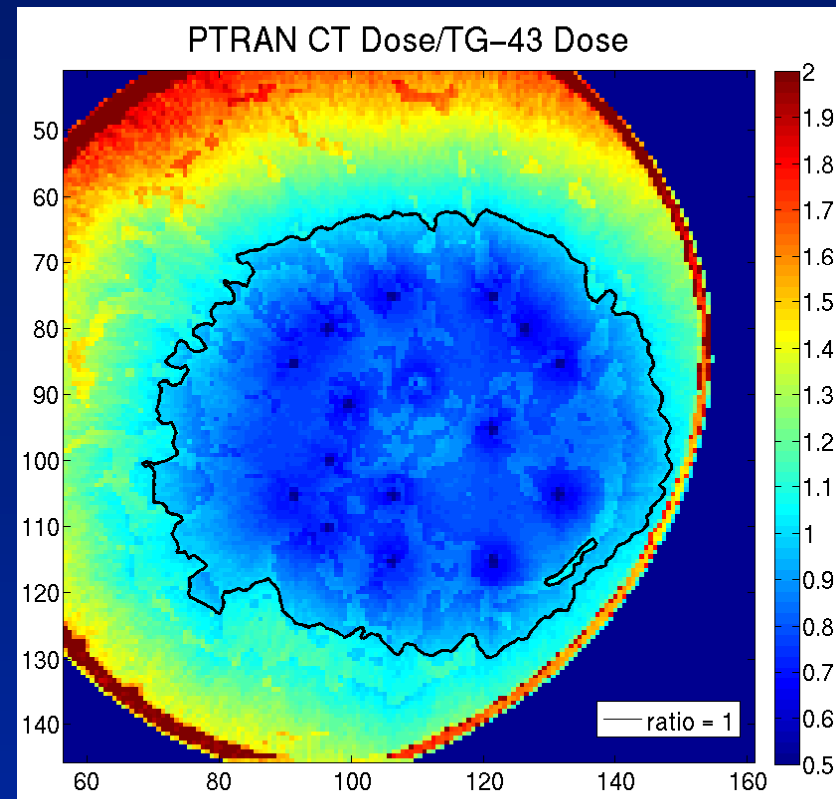
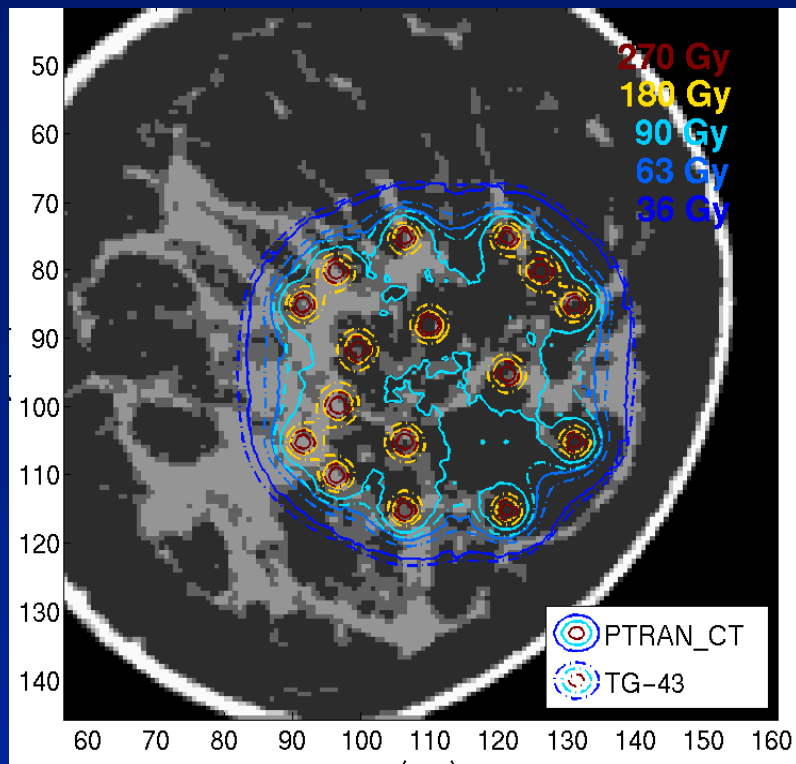
## Monte Carlo uncertainties: Model 6711 seed in liquid water

Distance	1 cm	5 cm	10 cm
Statistics	0.2%	0.3%	0.7%
Photon cross-sections	0.7%	2.4%	4.1%
Seed geometry	1.1%	0.9%	0.8%
Source energy spectrum	0.2%	0.3%	0.5%
Combined std. uncertainty ( $k=1$ )	1.3%	2.6%	4.3%

Adapted from Dolan et al. Med Phys 2006

# Monte Carlo-based Treatment planning

## Consolidating Dosimetry and treatment planning into a single process



- Permanent seed APBI: 70  $^{125}\text{I}$  seeds,  $D_{90} = 115 \text{ Gy}$
- 0.7 mm voxels, average SD = 1.2%, single-processor CPU time = 30 min

# Monte Carlo vs TLD

- **Measurement Pros and Cons**
  - Large uncertainties and many artifacts
  - Tests conjunction of all a priori assumptions: geometry, detector response corrections, calibration etc
- **Monte Carlo Pros and Cons**
  - Artifact-free, low uncertainty, and unlimited spatial resolution
  - Garbage in-Garbage out
    - » Seed geometry errors
    - » Will not anticipate contaminant radionuclides etc.,  $S_K$  errors
  - Does not model detector signal formation process
- **Hence: TG-43 continues to require both measured and Monte Carlo single-seed dose distributions**

# Dosimetry: Conclusions

- **Low energy brachytherapy: main catalyst for improving dosimetry and source standardization for 30 years**
  - Single-source dose distributions have 5% uncertainty
  - Both MC and measurement have important roles
- **Current Role**
  - Monte Carlo: primary source of dosimetric data
    - » Soon: MC dosimetry and planning will be a single process
  - Measurement: Confirm Monte Carlo assumptions
- **Major needs: more accurate and efficient dose-measurement systems for low energy sources**
  - Test batch-to-batch and/or source-to-source variations during manufacturing process